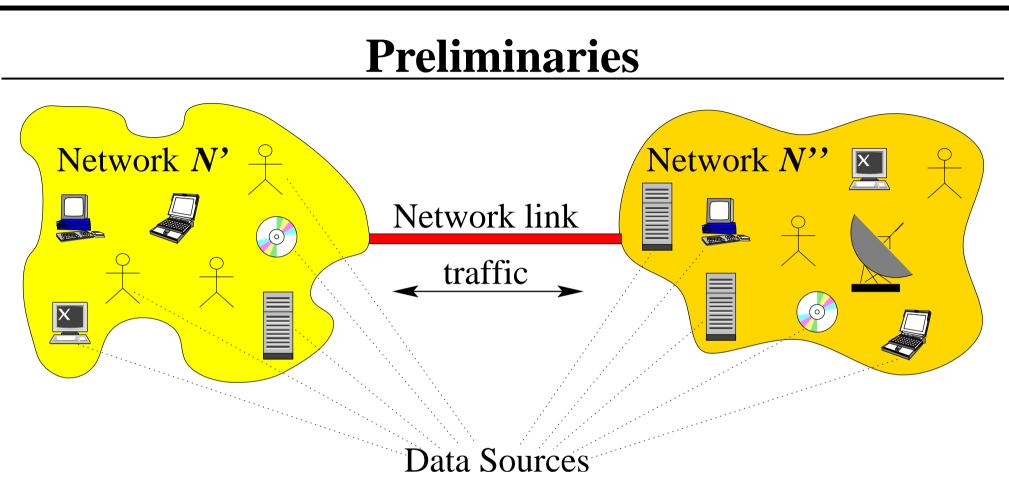


# On the Problem of Modeling and Identification for Traffic Structure of a Network Link

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Data *sources* send data to the *link*. All data are multiplexed and form *traffic* of the link.

Are there invariants—traffic structure?

## **Two-Component Description of Traffic**

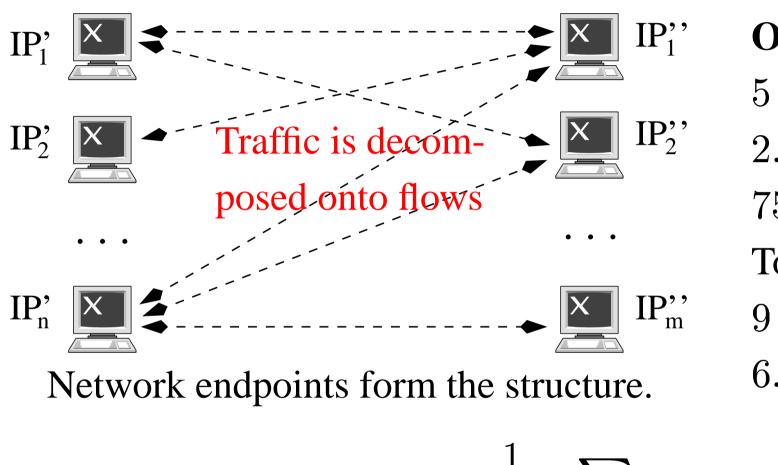
**Model:**  $| \text{traffic} | = | \text{structure } S | + | \text{stochastic } \mathcal{P}$ 

Structure: invariant rules of traffic forming
Stochastic: changeability of traffic

Structural model of a traffic characteristic (e.g. throughput):  $V(\Delta) = F_{\mathbb{S}}(x_1(\mathcal{P}), \dots, x_m(\mathcal{P}))$ 

 $V(\Delta)$  is modeled variable on time interval  $\Delta$  $x_i$  are input (measured) parameters (e.g. data volumes)





 Observations:

 5 month,

  $2.5 \cdot 10^6$  IPs,

 75.9 Mb/day,

 Total 1.8 Tb,

  $9 \cdot 10^8$  flows,

  $6.7 \cdot 10^9$  packets

Troughput(
$$\Delta$$
) =  $\frac{1}{\Delta} \sum_{(\mathrm{IP}'_i, \mathrm{IP}''_j)} v(\mathrm{IP}'_i, \mathrm{IP}''_j)$ 

# **Aggregated Data Sources**

- The number of real sources is too large
- Heterogenous sources should be classified
- Model should be simple and compact

Troughput(
$$\Delta$$
) =  $\sum_{s \in \mathcal{H}} \nu_s(\Delta) v_s$ 

 $\nu_s(\Delta)$  — activity of the aggregated source s $v_s$  — permanent characteristic of the aggregated source s

How real sources can be transformed to aggregated ones?

### **Model Identification Problem**

 $x = (x_1(\Delta), x_2(\Delta), \dots, x_m(\Delta))$  is classified data volumes

**Hypothesis:** there exists a linear Diophantine system  $\forall \Delta$ 

$$Ax = \mathbb{O}, \quad A \in \mathbb{Z}^{n \times m}, \quad x \in \mathbb{Z}_{+}^{m}$$
(1)

**Model:** Troughput(
$$\Delta$$
) =  $\sum_{s \in \mathcal{H}} \nu_s(\Delta) h^{(s)}$ ,  
where  $\mathcal{H} = \{h^{(1)}, \dots, h^{(q)}\}$  is Hilbert basis of (1)

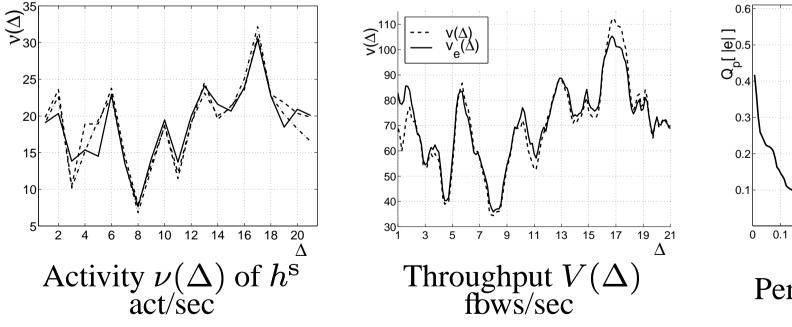
**Problems:** 

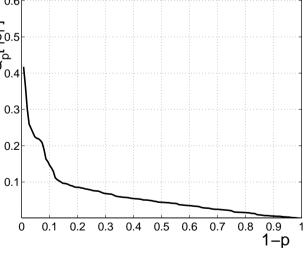
- equality in (1) is approximate and scalable
- identification of the matrix A
- searching  $\mathcal{H}$  and  $\nu_s(\Delta)$

#### **Experiment confirmation**

Classification: 6 groups by volume of flowsGr.1Gr.2Gr.3Gr.4Gr.5Gr.6 $[0, 100), [100, 500), [500, 10^3), [10^3, 5 \cdot 10^3), [5 \cdot 10^3, 10^4), [10^4, +\infty)$ 

# Principal aggregated sources: $h^{(v)} = (0, 0, 0, 2, 1, 1),$ $h^{(m)} = (0, 0, 1, 2, 0, 0), \quad h^{(s)} = (1, 1, 1, 0, 0, 0)$





Percentile of abs.err.

#### Conclusion

- 1. Discrete model of traffic structure is proposed
- 2. The model identification is based on a linear Diophantine system construction and Hilbert basis searching
- Our experiments confirm the applicability of the model (existence of stable aggregated sources, compactness, scalability, representativeness)